

RSA Encryption

$$n = p * q$$

$$\phi(n) = (p-1)(q-1)$$

$$\gcd(\phi(n), e) = 1 \quad // \text{ This is where I should use Euklide Extended Algorithm}$$

$$d * e \equiv 1 \pmod{\phi(n)}$$

Public key: (e, n)

Private key: (d, n)

Encryption:

$$C = M^e \pmod{n}$$

Decryption:

$$M = C^d \pmod{n}$$

$$p=3, q=11, e=7, M=5$$

$$n = 3 * 11 = 33$$

$$\phi(n) = 2 * 10 = 20$$

$$\gcd(20, 3) = 1$$

$$3 * 7 \equiv 1 \pmod{20}$$

a) Public key: $(7, 33)$
Private key: $(3, 33)$

Encryption:

$$C = 5^7 \pmod{33} = 14$$

Decryption:

$$M = 14^3 \pmod{33}$$

$$p=5, q=11, e=3, M=9$$

$$n = 5 * 11 = 55$$

$$\phi(n) = 4 * 10 = 40$$

$$\gcd(40, 3) = 1$$

$$27 * 3 \equiv 1 \pmod{40}$$

b) Public key: $(3, 55)$
Private key: $(27, 55)$

Encryption:

$$C = 9^3 \pmod{55} = 14$$

Decryption:

$$M = 14^{27} \pmod{55} = 9$$

$$p=7, q=11, e=17, M=8$$

$$n = 7 * 11 = 77$$

$$\phi(n) = 6 * 10 = 60$$

$$\gcd(60, 17) = 1$$

$$68 * 17 \equiv 1 \pmod{60}$$

c) Public key: $(17, 77)$
Private key: $(68, 77)$

Encryption:

$$C = 8^{17} \pmod{77} = 32$$

Decryption:

$$M = 32^{68} \pmod{77} = 8$$

a)

Euclides Exteded Algorithm in a)

$$\gcd(20, 3) = 1$$

$$20 = 3 * 6 + 2$$

$$3 = 2 * 1 + 1 \quad // \text{ Use this forumla and convert it to } 1 = 3 - 2 * 1$$

$$1 = 3 - 2 * 1$$

$$1 = 3 - (20 - 3 * 6) \quad // \text{ Now what? I don't remember from here. The answer is 3, the private key...}$$